

Duality, non-renormalization, superblocks and lines of CFTs without SUSY

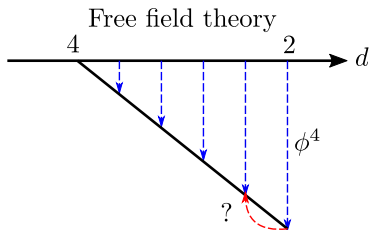
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Collaborators: Rastelli, Rychkov, Zan
[1703.05325](https://arxiv.org/abs/1703.05325), [1810.07199](https://arxiv.org/abs/1810.07199)

Epsilon expansions

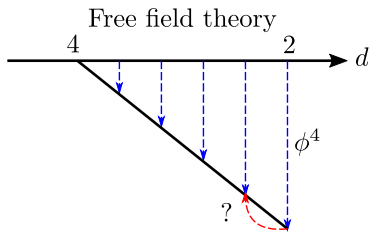


Expansion in $\varepsilon = 4 - d$:

$$S = \int \frac{1}{2} \phi \partial^2 \phi + \frac{\lambda}{4!} \phi^4 d^d x$$

Expansion in $\delta = d - 2$: ???

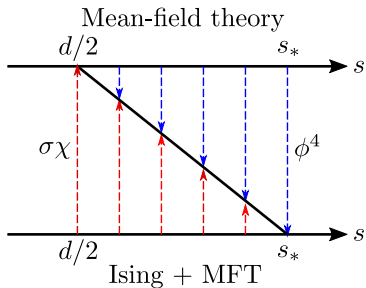
Epsilon expansions



Expansion in $\varepsilon = 4 - d$:

$$S = \int \frac{1}{2} \phi \partial^2 \phi + \frac{\lambda}{4!} \phi^4 d^d x$$

Expansion in $\delta = d - 2$: ???



Expansion in $\varepsilon = 2s - d$:

$$S = \int \frac{1}{2} \phi \partial^s \phi + \frac{\lambda}{4!} \phi^4 d^d x$$

Expansion in $\delta = \frac{s_* - s}{2}$:

$$S = S_{\text{Ising}} + \int \frac{1}{2} \chi \partial^{-s} \chi + g \sigma \chi d^d x$$

Features of the duality

Matching operators:

$$\begin{aligned}\phi &\leftrightarrow \sigma & \phi^4 &\leftrightarrow \sigma\chi \\ \phi^2 &\leftrightarrow \epsilon & [\phi\phi]_{0,2}^{\mu\nu} &\leftrightarrow T^{\mu\nu} \\ \phi^3 &\leftrightarrow \chi & \partial_\nu[\phi\phi]_{0,2}^{\mu\nu} &\leftrightarrow [\sigma\chi]_{0,1}^\mu\end{aligned}$$

Exact dimensions:

$$\begin{aligned}\Delta_\phi = \frac{d-s}{2} = d - \Delta_{\phi^3} &, \quad \Delta_\sigma = \frac{d-s}{2} = d - \Delta_\chi \\ \partial^s \phi = \phi^3 &, \quad \partial^{-s} \chi = \sigma\end{aligned}$$

Approximate dimensions:

$$\begin{aligned}\gamma_\epsilon^{(2)} &= 0.27\delta, \quad \gamma_{\phi^2}^{(2)} = \left[\psi(1) - 2\psi\left(\frac{d}{4}\right) + \psi\left(\frac{d}{2}\right) \right] \left(\frac{\epsilon}{3}\right)^2 \\ \gamma_T^{(2)} &= 2.33\delta, \quad \gamma_{[\phi\phi]_{0,2}}^{(2)} = -\frac{8}{d(d+2)} \left(\frac{\epsilon}{3}\right)^2\end{aligned}$$

Exciting stuff

$\langle \mathcal{O}_1 \mathcal{O}_2 \chi \rangle$ can be explicitly computed in terms of $\langle \mathcal{O}_1 \mathcal{O}_2 \sigma \rangle$.

$$\lambda_{12\chi} \lambda_{34\sigma} = \frac{\Gamma\left(\frac{\Delta_\chi \pm \Delta_{12} + \ell_1 + \ell_2 - 2m}{2}\right) \Gamma\left(\frac{\Delta_\sigma \pm \Delta_{34} + \ell_1 + \ell_2 - 2m}{2}\right)}{\Gamma\left(\frac{\Delta_\sigma \pm \Delta_{12} + \ell_1 + \ell_2 - 2m}{2}\right) \Gamma\left(\frac{\Delta_\chi \pm \Delta_{34} + \ell_1 + \ell_2 - 2m}{2}\right)} \lambda_{12\sigma} \lambda_{12\chi}$$
$$\lambda_{\sigma\chi\mathcal{O}}^2 = \frac{\Gamma\left(\frac{d-\Delta+\ell}{2}\right)^2 \Gamma\left(\frac{d-2\Delta_\sigma+\Delta+\ell}{2}\right) \Gamma\left(\frac{2\Delta_\sigma-d+\Delta+\ell}{2}\right)}{\Gamma\left(\frac{\Delta+\ell}{2}\right)^2 \Gamma\left(\frac{2\Delta_\sigma-\Delta+\ell}{2}\right) \Gamma\left(\frac{2d-2\Delta_\sigma-\Delta+\ell}{2}\right)} \lambda_{\sigma\sigma\mathcal{O}} \lambda_{\chi\chi\mathcal{O}}$$

Protected operators for odd ℓ , superblocks for even ℓ !

